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**Jiazuo Zhou\*** (zhoujz@swu.edu.cn), School of Mathematics and Statistics, Southwest University, Chongqing, 400715, Peoples Rep of China, and **Deshuo Jiang**, School of Math. and Statis, Wuhan University, Wuhan, 430072, Peoples Rep of China. *The Ros' theorem for convex domain*. Preliminary report.

Let  $\Sigma$  be a compact embedded hypersurface surface in  $R^n$  bounding a domain  $D$  of volume  $V$ . If the mean curvature  $H$  of  $\Sigma$  is positive everywhere, then we have the Ros' inequality:

$$\int_{\Sigma} \frac{1}{H} dA \geq nV,$$

where  $dA$  is the volume element of  $\Sigma$ . Equality holds when  $\Sigma$  is a standard  $(n-1)$ -sphere. For the case of  $R^3$ , the equality holds if and only if the surface  $\Sigma$  is the unit sphere. The Ros' theorem (when  $n=3$ ) has been reproved and generalized to higher dimensions by known mathematicians. If we consider the convex bodies with the smooth boundaries in  $\mathbb{R}^n$  the proof of the Ros's theorem would be simplified. We have a more stronger results than Ros'.

**Theorem.** *Let  $\Sigma$  be a compact embedded convex hypersurface in  $R^n$  bounding a convex body  $K$  of volume  $V$  and area  $A$ . Let  $W_2$  be the second Minkowski quermassintegrals of  $K$ . If the mean curvature  $H$  of  $\Sigma$  is positive everywhere, then*

$$\int_{\Sigma} \frac{1}{H} dA \geq \frac{A^2}{nW_2}. \tag{1}$$

*Equality holds if and only if  $\Sigma$  is a standard hypersphere.*

One may conjecture that the positivity of the mean curvature would be stronger enough to guarantee the convexity of the domain. (Received February 01, 2007)