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**Cormac O’Sullivan** and **Anthony Weaver\*** ([anthonyweaver@mac.com](mailto:anthonyweaver@mac.com)), University Ave and West 181st St., Bronx, NY 10453. *The largest non-genus of  $\mathbb{Z}_{pq}$  and the Frobenius problem.* Preliminary report.

Finite groups, all of whose  $p$ -Sylow subgroups are cyclic, act on curves of all but finitely many genera. For such groups it is natural to ask for the *largest non-genus*, that is, the largest nonnegative integer  $g$  such that the group does not act on a curve of genus  $g$ . The general problem is very difficult. It is related (but not quite equivalent) to a ( $d$ -dimensional) *Frobenius problem*: given a set of  $d > 1$  positive integers, all  $> 1$ , with greatest common divisor = 1, find the largest positive integer that cannot be represented as a positive integral linear combination of the integers in the given set. A general formula is known only when  $d = 2$ .

A formula for the largest non-genus of the (non-cyclic) metacyclic group of order  $pq$  was obtained by one of us (Weaver) in 2001. That case was easier because (i) there is the restriction that  $p \equiv 1 \pmod{q}$ , and (ii) the associated Frobenius problem is 3-dimensional. Here we determine the largest non-genus of  $\mathbb{Z}_{pq}$ , and solve the associated 4-dimensional Frobenius problem, in the cases where  $q$  is sufficiently large (on the order of  $2p^2$ ) with respect to  $p$ . We do the same for a large class of cases in which  $q \leq 2p - 1$ . This includes the class of twin primes. (Received February 01, 2007)