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*Tridiagonal pairs and the  $q$ -tetrahedron algebra.*

Let  $K$  denote a field and let  $V$  denote a vector space over  $K$  with finite positive dimension. By a *Leonard pair* on  $V$  we mean an ordered pair of linear transformations  $A : V \rightarrow V$  and  $A^* : V \rightarrow V$  that satisfy the following:

1. There exists a basis for  $V$  with respect to which the matrix representing  $A$  is diagonal and the matrix representing  $A^*$  is irreducible tridiagonal;
2. There exists a basis for  $V$  with respect to which the matrix representing  $A^*$  is diagonal and the matrix representing  $A$  is irreducible tridiagonal.

It is known that the Leonard pairs are in bijection with the orthogonal polynomials from the terminating branch of the Askey scheme. This branch includes the  $q$ -Racah polynomials and their relatives. In this talk we consider a mild generalization of a Leonard pair called a *tridiagonal pair*. We also consider the  $q$ -tetrahedron algebra, which can be viewed as a  $q$ -analog of the three-point  $\mathfrak{sl}_2$  loop algebra. We obtain a tridiagonal pair from each finite-dimensional irreducible module for the  $q$ -tetrahedron algebra. (Received February 13, 2007)