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**Harout Aydinian** and **Éva Czabarka\*** (czabarka@math.sc.edu), Department of Mathematics, Columbia, SC 29208, and **Péter L Erdős** and **László Székely**. *M-part L-Sperner families*. Preliminary report.

Let  $X = X_1 \cup X_2 \cup \cdots \cup X_M$  be a partition of the  $n$ -element underlying set  $X$ . A set system  $\mathcal{F} \subseteq 2^X$  is an  $M$ -part Sperner family if for all  $E, F \in \mathcal{F}$  such that  $E$  is a strict subset of  $F$ ,  $F \setminus E$  is not a subset of any of the  $X_i$ . It is known (Kleitman, 1965; Katona, 1960) that the size of a 2-part Sperner family cannot exceed the maximum size of a Sperner family,  $\binom{n}{\lfloor n/2 \rfloor}$ . However, for  $M > 2$  the situation is quite different, and the maximum size of a family is unknown in the general case.

$\mathcal{F}$  is an  $M$ -part  $L$ -Sperner family if for any chain  $E_1 \subset E_2 \subset \cdots \subset E_{L+1}$  of size  $L + 1$  in the family,  $E_{L+1} \setminus E_1$  is not a subset of any of the  $X_i$ . Füredi, Griggs, Odlyzko and Shearer (1987) determined the maximum size of such a family for  $M = L = 2$  and posed the question of maximal size in the general case.

We define  $\mathcal{F}$  is an  $M$ -part  $L_1, L_2, \dots, L_M$ -Sperner family if for any  $j \in \{1, \dots, M\}$  for any chain  $E_1 \subset E_2 \subset \cdots \subset E_{L_j+1}$  of size  $L_j + 1$  in the family,  $E_{L_j+1} \setminus E_1$  is not a subset  $X_j$ .

We will present some results and conjectures about these generalizations. (Received August 07, 2007)