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**Pierre Germain** and **Natasa Pavlovic\*** ([natasa@math.princeton.edu](mailto:natasa@math.princeton.edu)), Department of Mathematics, The University of Texas at Austin, 1 University Station, C1200, Austin, TX 78712, and **Gigliola Staffilani**. *Regularity of solutions to the Navier-Stokes equations evolving from small initial data in a critical space.*

In this talk we will present a regularity result for solutions to the Navier-Stokes equations evolving from small initial data in a critical space in  $\mathbb{R}^n$ .

More precisely, in 2001 H. Koch and D. Tataru proved the existence of global in time solutions to the incompressible Navier-Stokes equations in  $\mathbb{R}^n$  corresponding to the initial data small enough in  $BMO^{-1}$ . We prove that under certain smallness condition on the initial data in  $BMO^{-1}$ , the solutions constructed by Koch and Tataru are more regular. As a consequence, we obtain a decay estimate in time for any space derivative, and space analyticity of the solution. Also as an application of our regularity theorem, we prove a regularity result for self-similar solutions. (Received July 24, 2007)