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Let  $X$  be a nonempty set,  $\Gamma$  a field of subsets of  $X$ , and  $\mathcal{K} = (K_n)$  be an increasing sequence of subsets of  $X$  such that  $K_0$  is nonempty and  $X = \cup_n K_n$ . A density  $\mu : \Gamma \rightarrow [0, 1]$  with  $\mathcal{K}$ -null sets is a finitely additive function with the properties that subsets of null sets are null sets,  $\mu(X) = 1$ , and, if  $A \subset K_n$  for some  $n$ , then  $\mu(A) = 0$ . Densities need not be countably additive, but may exhibit the *additive property*, i.e., given an increasing sequence of sets  $\langle A_n \rangle$ ,  $A_n \in \Gamma$  for all  $n$ , there is a set  $A \in \Gamma$  such that  $A \setminus A_n$  is subset of an element of  $\mathcal{K}$  and  $\mu(A) = \lim_n \mu(A_n)$ . It is known that regular summability methods generate densities on  $\mathbf{N}$  that have the additive property. Densities on  $\mathbf{N} \times \mathbf{N}$  generated by RH regular methods need not have the additive property. We also discuss a method for using regular summability methods to create densities on  $\mathbf{N} \times \mathbf{N}$  that have the additive property. (Received August 03, 2007)