

1030-42-203

**Ebner Pineda** (ebner.pineda@gmail.com), Universidad Centroccidental Lisandro Alvarado, Decanato de Ciencias y Tecnologia, Departamento de Matemáticas, Barquisimeto, Edo Lara, Venezuela, and **Wilfredo O Urbina\*** (wilfredo.urbina@gmail.com), DePaul University, Department of Mathematical Sciences, 2320 North Kenmore Ave., Chicago, IL 60614. *On Besov-Lipschitz spaces for Hermite polynomial expansions for any  $\alpha > 0$ .*

We consider the Besov-Lipschitz spaces  $B_{p,q}^\alpha(\gamma_d)$  for Hermite polynomial expansions for any  $\alpha > 0$ , defined as the set of functions  $f \in L^p(\gamma_d)$  for which

$$\int_0^\infty (t^{k-\alpha} \left\| \frac{\partial^k u(\cdot, t)}{\partial t^k} \right\|_{p,\gamma_d})^q \frac{dt}{t} < \infty, \quad (1)$$

where  $k$  be the smallest integer greater than  $\alpha$  and  $1 < p, q < \infty$ ,  $u(x, t) = P_t f(x)$  and  $\{P_t\}_{t \geq 0}$  is the Poisson-Hermite semigroup,

In order to this definition makes sense it is needed to prove that if  $k, l$  integers greater than  $\alpha$ , then

$$\left\| \frac{\partial^k u(\cdot, t)}{\partial t^k} \right\|_{p,\gamma} \leq A_k t^{-k+\alpha} \text{ if and only if } \left\| \frac{\partial^l u(\cdot, t)}{\partial t^l} \right\|_{p,\gamma} \leq A_l t^{-l+\alpha}.$$

Also we prove some inclusions among those spaces. (Received August 02, 2007)