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Xiaochun Li* (xcli@math.uiuc.edu), Department of Mathematics, University of Illinois at Urbana-Champaign, Urbana, IL 61801. *Bilinear oscillatory integrals along curves*. Preliminary report.

We discuss some bilinear oscillatory integrals along some curves such as polynomial curves.

For example, let $T(f, g)$ be defined by

$$T_\beta(f, g)(x) = p.v \int_{-1}^1 f(x-t)g(x-t^2)e^{1/|t|^\beta} \frac{dt}{t}.$$

We ask whether T_β maps $L^p \times L^q$ to L^r for some p, q, r .

It turns out that such problems are related to the trilinear oscillatory integrals. If $\beta > 6$ we can obtain that T_β is bounded from $L^p \times L^q$ to L^r for all $p, q > 1$ and $1/r = 1/p + 1/q$. It is still open when $0 < \beta < 6$. This is a joint work with D. Fan. (Received August 06, 2007)