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**Carlos Prez\*** ([carlosperez@us.es](mailto:carlosperez@us.es)), Department of Mathematics, Kansas University, Lawrence, KS 66045-7523, and **Andrei Lerner** and **Sheldy Ombrosi**. *Sharp  $A_1$  bounds for Caldern-Zygmund operators and the relationship with a problem of Muckenhoupt and Wheeden.*

For any Caldern-Zygmund operator  $T$  we prove sharp weighted  $L^p$  estimates when the weight satisfies the  $A_1$  condition within the range  $1 < p < \infty$ . In the case when  $p = 2$  and  $T$  is a classical convolution singular integral, this result is due to R. Fefferman and J. Pipher. Our method is different avoiding Littlewood-Paley square functions. Using this estimate we will sketch, assuming again that  $w \in A_1$  how to deduce a weighted weak type  $(1, 1)$  estimate with some logarithmic loss. It seems that this estimate is not sharp but it is related to a conjecture of Muckenhoupt and Wheeden that we will address. (Received August 06, 2007)