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**Maria Alfonseca\***, 300 Minard Hall, Department of Mathematics, Fargo, ND 58105, and  
**Dmitry Ryabogin** and **Artem Zvavitch**. *Radially symmetric intersection bodies with an  
(n-1)-dimensional face*. Preliminary report.

Intersection bodies appear as dual of zonoids. It is not known if a zonoid whose dual is also a zonoid may have an (n-1)-dimensional symmetric face in dimensions 5 and higher. The existence or not of such examples is related to an isometric analogue of a theorem of Grothendieck that states that the only infinite-dimensional Banach spaces that are isometric to both a subspace of  $L^1$  and a quotient space of  $L^\infty$  are isomorphic to a Hilbert space.

Approaching the problem from the intersection body setting, we construct examples of radially symmetric intersection bodies that have an (n-1)-dimensional symmetric face and we investigate if their duals are zonoids. (Received August 07, 2007)