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It was shown by P. Erdős that if t is a *real* trigonometric polynomial of degree n such that $|t(x)| \leq 1$ for all real x , then the arc-length of its graph on any interval of length 2π cannot exceed that of $\cos nx$. This result was generalized by A.P. Calderon and G. Klein who proved that $\int_{-\pi}^{\pi} \varphi(|t'(x)|) dx \leq \int_{-\pi}^{\pi} \varphi(|-n \sin nx|) dx$ if $\varphi : [0, \infty) \rightarrow \mathfrak{R}$ is such that $(\varphi(u) - \varphi(0))/u$ is a non-decreasing function of u on $(0, \infty)$. In particular, for any a , the integral $\int_a^{a+2\pi} |t'(x)|^p dx$ cannot be larger than the corresponding integral for $t(x) := \cos nx$, if $p \geq 1$. We note that the restriction on p in this result can be relaxed. In addition, we formulate and prove an extension of the theorem of Calderon and Klein to non-periodic entire functions of exponential type. (Received June 17, 2007)