

1032-42-207

George C. Stey* (gcstey@windstream.net), Mathematics Building, 121A, 231 West 18th Ave, Columbus, OH 43210. *Behavior of the Norm of N-Fold Convolutions.*

Define $g_1(x) = g(x)$, $g_{n+1}(x) = \int_{-\infty}^{\infty} g(x-y)g_n(y)dy$, $n = 1, 2, 3, \dots$. Under four assumptions on $g(x)$ and its Fourier transform, $\hat{g}(t)$, which imply that there be only one point, t_0 , at which $|\hat{g}(t_0)| = \sup_{s \in \mathbb{R}} |\hat{g}(s)|$ and that $0 < \text{Re}(K_2)$, where $K_j = (-id/dt)^j \ln(\hat{g}(t))|_{t=t_0}$, it has been shown (G.C. Stey, dissertation, Ohio State U., 2007) that $\|g_n\|_{L^1} = |\hat{g}(t_0)|^n \{ \sum_{\ell=0}^L c_\ell (\frac{1}{n})^\ell + o((\frac{1}{n})^L) \}$ as $n \rightarrow \infty$, ($L = 1, 2, 3, \dots$),

where $c_\ell = \frac{1}{\sqrt{2\pi|K_2|}} \int_{-\infty}^{\infty} e^{\{-w^2 \text{Re}(\frac{1}{2K_2})\}} S_{2\ell}(w) dw$, where $S_0(w) = 1 = Q_0(w)$,

$S_r(w) = \sum_{m=1}^r m! \binom{1/2}{m} \Sigma'_{(m_1, m_2, \dots, m_r), m} \prod_{j=1}^r [\sum_{j_1=0}^j Q_{j-j_1}(w) \bar{Q}_{j_1}(w)]^{m_j} / m_j!$, with

$Q_r(w) = \sum_{m=1}^r He_{2m+r}(\frac{-w}{\sqrt{K_2}}) \Sigma'_{(m_1, m_2, \dots, m_r), m} \prod_{j=1}^r \{ (\frac{1}{\sqrt{K_2}})^{2+j} \frac{K_{2+j}}{(2+j)!} \}^{m_j} / m_j!$ ($r = 1, 2, 3, \dots$), $He_k(u) = \exp(u^2/2) (-d/du)^k \exp(-u^2/2)$, and Σ' indicates $\sum_{j=1}^r m_j = m$ and $\sum_{j=1}^r j m_j = r$, with nonnegative integers m_j . (Received August 22, 2007)