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**George C. Stey\*** (gcstey@windstream.net), Mathematics Building, 121A, 231 West 18th Ave, Columbus, OH 43210. *Behavior of the Norm of N-Fold Convolutions.*

Define  $g_1(x) = g(x)$ ,  $g_{n+1}(x) = \int_{-\infty}^{\infty} g(x-y)g_n(y)dy$ ,  $n = 1, 2, 3, \dots$ . Under four assumptions on  $g(x)$  and its Fourier transform,  $\hat{g}(t)$ , which imply that there be only one point,  $t_0$ , at which  $|\hat{g}(t_0)| = \sup_{s \in \mathbb{R}} |\hat{g}(s)|$  and that  $0 < \text{Re}(K_2)$ , where  $K_j = (-id/dt)^j \ln(\hat{g}(t))|_{t=t_0}$ , it has been shown (G.C. Stey, dissertation, Ohio State U., 2007) that  $\|g_n\|_{L^1} = |\hat{g}(t_0)|^n \{ \sum_{\ell=0}^L c_\ell (\frac{1}{n})^\ell + o((\frac{1}{n})^L) \}$  as  $n \rightarrow \infty$ , ( $L = 1, 2, 3, \dots$ ),

where  $c_\ell = \frac{1}{\sqrt{2\pi|K_2|}} \int_{-\infty}^{\infty} e^{\{-w^2 \text{Re}(\frac{1}{2K_2})\}} S_{2\ell}(w) dw$ , where  $S_0(w) = 1 = Q_0(w)$ ,

$S_r(w) = \sum_{m=1}^r m! \binom{1/2}{m} \Sigma'_{(m_1, m_2, \dots, m_r), m} \prod_{j=1}^r [\sum_{j_1=0}^j Q_{j-j_1}(w) \bar{Q}_{j_1}(w)]^{m_j} / m_j!$ , with

$Q_r(w) = \sum_{m=1}^r He_{2m+r}(\frac{-w}{\sqrt{K_2}}) \Sigma'_{(m_1, m_2, \dots, m_r), m} \prod_{j=1}^r \{ (\frac{1}{\sqrt{K_2}})^{2+j} \frac{K_2+j}{(2+j)!} \}^{m_j} / m_j!$  ( $r = 1, 2, 3, \dots$ ),  $He_k(u) = \exp(u^2/2) (-d/du)^k \exp(-u^2/2)$ , and  $\Sigma'$  indicates  $\sum_{j=1}^r m_j = m$  and  $\sum_{j=1}^r j m_j = r$ , with nonnegative integers  $m_j$ . (Received August 22, 2007)