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Let  $X$  be a contraction operator on a Hilbert space  $\mathcal{A}$  defined on a linear subspace  $\mathcal{B} \subseteq \mathcal{A}$ . A weak unitary dilation of  $X$  is a unitary operator  $U$  defined on a Hilbert space  $\tilde{\mathcal{A}} \supseteq \mathcal{A}$  such that  $P_{\mathcal{A}}U|_{\mathcal{B}} = X$ . A weak unitary dilation  $U$  on  $\tilde{\mathcal{A}}$  is said to be minimal if  $\mathcal{A}$  is cyclic for  $U$ . Two minimal weak unitary dilations of  $X$ , say  $U$  on  $\tilde{\mathcal{A}}$  and  $U'$  on  $\tilde{\mathcal{A}}'$ , are regarded as indistinguishable whenever there exists a unitary operator  $\Phi : \tilde{\mathcal{A}} \rightarrow \tilde{\mathcal{A}}'$  such that  $\Phi|_{\mathcal{A}} = 1$  and  $\Phi U = U' \Phi$ . We present a description of the minimal weak unitary dilations of  $X : \mathcal{B} \rightarrow \mathcal{A}$  in terms of a class of Schur functions. The derived functional model may be used to parametrize the interpolants in the Relaxed Commutant Lifting Theorem in a similar way as the Arov-Grossman model yields a parametrization of the interpolants in the classical Sarason-Sz.-Nagy-Foias Commutant Lifting Theorem.

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