

1033-05-64

**Xiangqian Zhou\*** (zhx@marshall.edu), Department of Mathematics, Marshall University, Huntington, WV 25755, **Talmage J Reid**, 38677, and **Haidong Wu**. *On Minimally  $k$ -Connected Matroids*.

A graph  $G$  is *minimally  $k$ -connected* if  $G$  is  $k$ -connected and, for each edge  $e \in E(G)$ ,  $G \setminus e$  is not  $k$ -connected. Halin showed that a minimally  $k$ -connected graph has a vertex of degree  $k$ . The existence of vertices of degree  $k$  in minimally  $k$ -connected graphs has proven to be very useful in studying the structure of  $k$ -connected graphs.

A matroid  $M$  is *minimally  $k$ -connected* if  $M$  is  $k$ -connected, and for every  $e \in E(M)$ ,  $M \setminus e$  is not  $k$ -connected. It is conjectured that every minimally  $k$ -connected matroid with at least  $2(k-1)$  elements has a cocircuit of size  $k$ . For  $k = 2$  and 3, Murty (1974) and Wong (1978) resolved this conjecture affirmatively. We prove that a minimally 4-connected matroid has a cocircuit of size 4 unless it is isomorphic to a special matroid with 9 elements. We also construct a counterexample to the conjecture for each  $k \geq 5$ .

This is joint work with James Reid and Haidong Wu. (Received August 30, 2007)