

1036-20-95

**Ara Basmajian** and **Bernard Maskit\*** ([bernie@math.sunysb.edu](mailto:bernie@math.sunysb.edu)), Math. Dept., Stony Brook University, Stony Brook, NY 11794-3651. *Commutators in Groups of Hyperbolic Motions*. Preliminary report.

It is well known that, in dimensions 2 and 3, if  $A$  and  $B$  are orientation-preserving hyperbolic isometries, then we can find involutions  $\alpha$ ,  $\beta$  and  $\gamma$ , so that  $A = \alpha\beta$  and  $B = \beta\gamma$ ; then  $AB = \alpha\gamma$ , and the commutator  $[A, B^{-1}] = [\alpha\beta, \gamma\beta] = (\alpha\beta\gamma)^2$ . For higher dimensions, it is known that, in general, given  $A$  and  $B$ , one cannot find involutions  $\alpha$ ,  $\beta$  and  $\gamma$ , so that  $A = \alpha\beta$ , and  $B = \beta\gamma$ . However we do show that, in all dimensions  $ge2$ , given any orientation-preserving hyperbolic isometry  $C$ , there are involutions  $\alpha$ ,  $\beta$  and  $\gamma$ , so that  $C = (\alpha\beta\gamma)^2 = [\alpha\beta, \gamma\beta]$ . We also explore more specialized questions, such as: when can we write  $C$  in the form  $C = [A, B]$ , where  $A$  and  $B$  are conjugate involutions. (Received January 16, 2008)