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**Sudeb Mitra\*** (sudeb.mitra@qc.cuny.edu), Department of Mathematics, Queens College, CUNY, 65-30 Kissena Boulevard, Flushing, NY 11367-1597. *Some geometrical properties of the Teichmüller space of a Riemann surface rel a closed subset.* Preliminary report.

Let  $X$  be a hyperbolic Riemann surface (i.e. its universal covering surface is isomorphic to the upper half plane). Let  $E$  be a closed subset of  $X$ . The Teichmüller space of  $X$  rel  $E$ , denoted by  $T(X, E)$ , was first studied by Adam Epstein in his doctoral dissertation.

In this talk, we will discuss some geometrical properties of the space  $T(X, E)$ . We will show that the Teichmüller metric on  $T(X, E)$  is the same as its Kobayashi metric. We will then discuss how to extend Earle's sharp form of the principle of Teichmüller contraction to the space  $T(X, E)$ , and obtain a  $\delta, \epsilon$  form of Schwarz's lemma for holomorphic maps from the open unit disk to  $T(X, E)$ .

There is also a Teichmüller curve of  $X$  rel  $E$ , denoted by  $V(X, E)$ ; we will discuss some properties of the "simple holomorphic family"  $V(X, E) \rightarrow T(X, E)$  and outline an application to holomorphic motions. (Received December 30, 2007)