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**Rudi Pendavingh\*** (rud@win.tue.nl), TU/e, HG 9.30, Den dolech 2, P.O.Box 513, 5600MB Eindhoven, Netherlands, and **Stefan van Zwam**. *Partial fields and matroids with several inequivalent representations over  $GF(5)$ .*

et  $D := \{(-1)^s 2^t \mid s, t \in \mathbb{Z}\} \cup \{0\}$ . A matrix  $A$  is *dyadic* if the determinant of each submatrix of  $A$  is in  $D$ . A matroid is dyadic if it is represented by a dyadic matrix. A theorem of Whittle states that the following are equivalent for a matroid  $M$ :

1.  $M$  is dyadic;
2.  $M$  is representable over  $GF(3)$  and  $GF(5)$ ; and
3.  $M$  is representable over  $GF(p)$ , for  $p = 3$  and all  $p$  such that  $p = 2 \pmod{3}$ .

We present a lifting theorem for partial field homomorphisms. As a corollary we obtain Whittle's Theorem and a characterization of the matroids representable over  $GF(4)$  and  $GF(5)$  announced by Vertigan. We also characterize matroids with  $k$  representations over  $GF(5)$ .

Let  $G := \{i^a(1-i)^b \mid a, b \in \mathbb{Z}\} \cup \{0\}$ , where  $i$  is the complex unit. A matrix  $A$  is *Gaussian* if the determinant of each submatrix of  $A$  is in  $G$ . A matroid is Gaussian if it is represented by a Gaussian matrix. We show that if  $M$  is a 3-connected non-dyadic matroid, then the following are equivalent:

1.  $M$  is Gaussian;
2.  $M$  has two representations over  $GF(5)$ , and
3.  $M$  has two representations over  $GF(p)$ , for all  $p$  such that  $p = 1 \pmod{4}$ .

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