

1037-05-69

Alexandra Ovetsky Fradkin* (aovetsky@math.princeton.edu), Princeton University,
Department of Mathematics, Fine Hall, Washington Road, Princeton, NJ 08540. *Hadwiger's
conjecture for quasi-line graphs.*

Hadwiger's conjecture states that if a graph is not t -colorable then it contains the complete graph on $t+1$ vertices as a minor. The case $t=4$ is equivalent to the four color theorem and the case $t=5$ was proved by Robertson, Seymour, and Thomas with the use of the four color theorem. For $t>5$, the conjecture remains open. Reed and Seymour have also proved that Hadwiger's conjecture holds for line graphs.

A graph is a quasi-line graph if the neighbor set of every vertex is the union of two cliques. The class of quasi-line graphs is a proper superset of the class of line graphs. In a joint work with Maria Chudnovsky, we proved that Hadwiger's conjecture holds for quasi-line graphs, thus extending the result of Reed and Seymour. We used a structure theorem for quasi-line graphs from a recent work of Chudnovsky and Seymour. (Received January 22, 2008)