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Absolute minimizers of L -infinity functionals under the Dirichlet energy constraint. Preliminary report.

In this talk, I will describe a natural notion of absolute minimizer of

$$F(u, \Omega) = \|H(\nabla u)\|_{L^\infty(\Omega)}$$

subject to

$$D(u, \Omega) = \int_{\Omega} |\nabla u|^2 \leq E.$$

We prove that such an absolute minimizer is unique. This is achieved by showing roughly that

- (i) in $U_1 \equiv \Omega \cap \{x : H(\nabla u)(x) > \Lambda\}$, u is the (unique) absolute minimizer of H without constraint;
- (ii) in $U_2 \equiv \Omega \cap \{x : H(\nabla u)(x) \leq \Lambda\}$, u (uniquely) solves the Elastic-Plastic problem:

$$\min\{D(u, U_2) : H(\nabla u) \leq \Lambda\}.$$

This is joint work with Teng Jiang, based on his Ph.D. thesis. (Received January 22, 2008)