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Yuh-Jia Lee* (yjlee@nuk.edu.tw), Department of Applied Mathematics, National University of Kaohsiung, Kaohsiung, 811, Taiwan. *A Characterization of Lévy white noise measure.*

Let β be a positive finite measure on $(\mathbb{R}, \mathcal{B}(\mathbb{R}))$. For a Fréchet differentiable function φ on \mathcal{S}' , define $\partial_\eta \varphi$ as follows:

$$\partial_\eta \varphi(x) = \iint_{\mathbb{R}_*^2} \eta(t) \frac{\varphi(x + u\delta_t) - \varphi(x)}{u} \lambda(dt, du) + \sigma^2 \int_{-\infty}^{+\infty} \eta(t) D_{\delta_t} \varphi(x) dt,$$

where $\mathbb{R}_*^2 = \{(t, u) \in \mathbb{R}^2 : |u| > 0\}$, $\sigma^2 = \beta(\{0\})$ and $\lambda(dt, du) = (1 + u^2) \beta(du) dt$. Assume that β has finite second moment and there is a real constant τ such that for any functional φ in the algebra generated by $\{e^{i(\cdot, \eta)} : \eta \in \mathcal{S}\}$, the following equality holds:

$$\int_{\mathcal{S}'} \left((x, \zeta) - \tau \int_{-\infty}^{+\infty} \zeta(t) dt \right) \varphi(x) \Lambda(dx) = \int_{\mathcal{S}'} \partial_\zeta \varphi(x) \Lambda(dx), \quad \zeta \in \mathcal{S}. \quad (1)$$

It is shown that Λ is the Lévy white noise measure associated with the pair (μ, β) , where

$$\mu = \tau - \int_{-\infty}^{+\infty} u \beta(du).$$

Coversely if Λ is the Lévy white noise measure on \mathcal{S}' then (1) holds. (Received February 04, 2008)