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**Robert B Ellis\*** (rellis@math.iit.edu), 10 W. 32nd St., E1 Rm208, Chicago, IL 60616, and  
**James P Ferry**, 11911 Freedom Drive, Ste. 800, Reston, VA 20190. *Variance of the subgraph  
count for sparse Erdős-Rényi graphs.* Preliminary report.

We develop estimates for the variance of the number of copies of a small subgraph  $H$  in the Erdős-Rényi random graph by case analysis of the types of subgraphs  $H' \subseteq H$ . The central technique is a direct enumeration scheme which gives the asymptotic variance in the sparse case including constant average vertex degree. For a “small” number of vertices, we sharpen the enumeration scheme by classifying subgraphs  $H' \subseteq H$  and their contribution to the variance. This results in a bracketing of the small subgraph count variance for all parameters of the random graph. The estimate applies to a decision statistic for the detection of the insertion of  $H$  into the random graph by an adversary. (Received February 06, 2008)