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Zoltan Füredi* (z-furedi@math.uiuc.edu), Department of Mathematics, University of Illinois at Urbana-Champaign, 1409 W Green Street, Urbana, IL 61801. *Complete H -decompositions.*

Let H be a simple graph. An H -packing of order n is a set $\mathcal{P} := \{H_1, H_2, \dots, H_m\}$ of edge disjoint copies of H whose union forms a graph with n vertices. If this graph is the *complete graph* K_n , then \mathcal{P} is called a *perfect H -packing* on n vertices, or following the terminology of the design theory, it is called an *H -design* of order n . The case $H = K_k$ is equivalent to the existence of Steiner systems $S(n, k, 2)$.

Let $f(n; H)$ be the smallest integer t such that, any H -packing on n vertices can be extended to a perfect H -packing on at most $n + t$ vertices. The existence of $f(n; H)$ follows from a far more general result of Wilson 1972–1975.

There are many explicit constructions to provide linear upper bounds $f(n, H) < c_H n$ by Hoffman, Lindner, Rodger, and Stinson, by Jenkins, by Küçükçifçi, Lindner, and Rodger. Bryant, Khodkar, and El-Zanati gave explicit upper bounds (linear in n) for an infinite class of bipartite H .

Here we give an asymptotic that $f(n, C_4) = (1 + o(1))\sqrt{n}$. Most of this talk is based on work with Hilton, Lehel and Lindner. (Received February 06, 2008)