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**Mario Bonk\*** ([mbonk@umich.edu](mailto:mbonk@umich.edu)), University of Michigan, Ann Arbor, MI 48109.

*Postcritically-finite maps on the sphere.*

A continuous map  $f: S^2 \rightarrow S^2$  on the 2-sphere  $S^2$  is called topologically holomorphic if near each point it can be written as  $z \mapsto z^n$  for some  $n \in \mathbf{N}$  in suitable local coordinates in domain and image. The critical set of  $f$  is the set of all points where  $n \geq 2$ . The postcritical set is the forward orbit of the critical set under iteration of  $f$ . A topologically holomorphic map  $f: S^2 \rightarrow S^2$  is called postcritically finite if it has a finite postcritical set.

Thurston studied postcritically-finite maps and gave a necessary and sufficient condition for such a map to be equivalent (in a suitable sense) to a rational map. There is a close connection of this equivalence problem to the question when a metric 2-sphere is quasisymmetrically equivalent to the standard 2-sphere. In my talk I will give a survey on this subject and discuss some recent joint work with D. Meyer. (Received February 10, 2008)