

1039-47-9

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Linear Operators in Hypernormed Spaces. Preliminary report.

Let \mathbb{R}_ω be the set of all real hypernumbers and \mathbb{R}_ω^+ be the set of all real hypernumbers that are larger than or equal to zero [Burgin, M. Theory of Hypernumbers and Extrafunctions: Functional Spaces and Differentiation, *Discrete Dynamics in Nature and Society*, 7(3) 2002]. A hypernorm in a linear space L over the field \mathbb{R} is a mapping $|| \cdot || : L \rightarrow \mathbb{R}_\omega^+$ that satisfies the following axioms: N1. $||x|| = 0$ if and only if $x = 0$; N2. For any number a from \mathbb{R} , we have $||ax|| = |a| ||x||$; N3. $||x + y|| \leq ||x|| + ||y||$. Let us assume that E and L are hypernormed linear spaces and $A : E \rightarrow L$ is a linear operator. *Definition 1.* Operator A is called bounded if there is C from \mathbb{R} such that $||Ax|| \leq C ||x||$ for any x from E . *Definition 2.* Operator A is called continuous if for any sequence x_n with elements from E such that $\lim ||x_n|| = 0$, we have $\lim ||Ax_n|| = 0$. *Theorem 1.* A linear operator A is continuous if and only if it is bounded. (Received January 15, 2008)