

1041-05-101

**Daniel Panario\*** ([daniel@math.carleton.ca](mailto:daniel@math.carleton.ca)). *Smallest Components and Restricted Patterns in Combinatorial Decomposable Structures.*

We review the relation between objects and components in *decomposable combinatorial structures*. These structures consist of simpler entities called *components* which by themselves can not be further decomposed. Typical examples of these combinatorial structures are: permutations (decomposed into cycles), graphs (into connected components), and polynomials over finite fields (into irreducible factors).

The *restricted pattern* of an object of size  $n$  is a mapping  $S: J \mapsto \mathbb{N}$ , where  $J$  is a set of components' sizes,  $\mathbb{N}$  is the set of nonnegative integers, and  $S(j)$  is the number of components of size  $j$ . We want to count objects such that the components with sizes excluded from  $J$  may appear any number of times but there are exactly  $S(j)$  components of size  $j$ ,  $j \in J$ .

We survey several properties of smallest components, with and without restricted patterns. We assume that the component generating function  $C(z)$  is of *alg-log* type, that is,  $C(z)$  behaves like

$$(1 - z/\rho)^{-\alpha} \ln \left( \frac{1}{1 - z/\rho} \right)^{-\beta}$$

near its dominant singularity  $\rho$ . This includes the case when objects are in the so-called exp-log class. These concepts will be defined and examples will be given. (Received August 05, 2008)