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Sunil K Chebolu* (schebol@ilstu.edu), Department of Mathematics, Illinois State University, Campus box 4520, Normal, IL 61790, and **Jan Minac**. *A new interpretation of the quadratic closure of a field.*

Let F be a field that has a primitive p -th root of unity. The Bloch-Kato conjecture which has been recently proved by Voevodsky and Rost claims that the norm-residue map

$$K_*(F)/pK_*(F) \longrightarrow H^*(F, \mathbb{F}_p)$$

from the reduced Milnor K-theory to the Galois cohomology of F is an isomorphism. This gives a presentation of the rather mysterious Galois cohomology ring $H^*(F, \mathbb{F}_p)$ by generators and relations. In joint work with Minac, we have obtained (using the Bloch-Kato conjecture!) a second cohomology refinement of the Bloch-Kato conjecture. As a consequence we are able to characterise the quadratic closure of a field, and more generally, the maximal p -extension of F , as the “splitting field” for the Galois cohomology of the absolute Galois group. Together with Benson and Swallow we plan to study the higher cohomology refinements of the Bloch-Kato conjecture. (Received July 13, 2008)