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**James H. Schmerl\*** ([schmerl@math.uconn.edu](mailto:schmerl@math.uconn.edu)), Department of Mathematics, University of Connecticut, Storrs, CT 06269-3009.  *$\omega$ -models of Finite Set Theory.*

(This is joint work with Ali Enayat and Alber Visser.) Let  $\mathbf{ZF}_{\text{fin}}$  be the theory obtained from the usual formulation of  $\mathbf{ZF}$  by replacing the Axiom of Infinity with its negation. Within each model  $\mathfrak{M} \models \mathbf{ZF}_{\text{fin}}$  there is a naturally defined model  $\mathbb{N}^{\mathfrak{M}}$  of Peano Arithmetic. If  $\mathbb{N}^{\mathfrak{M}}$  is the standard model, then we say that  $\mathfrak{M}$  is an  *$\omega$ -model*. A method for constructing  $\omega$ -models of  $\mathbf{ZF}_{\text{fin}}$  will be presented, leading to results such as: (1) For each group  $G$  there is an  $\omega$ -model whose automorphism group is isomorphic to  $G$ . (2) For each infinite cardinal  $\kappa$ , there are  $2^\kappa$  nonisomorphic rigid  $\omega$ -models of cardinality  $\kappa$ . (3) There are infinitely many nonisomorphic, highly recursive, pointwise-definable  $\omega$ -models. In regard to (3),  $\mathfrak{M} = (M, E)$  is *highly recursive* if  $M$  and  $E$  are recursive and so is the function  $x \mapsto |\{y \in M : \langle y, x \rangle \in E\}|$ . In contrast to (3) there is: (4) Every recursive model of  $\mathbf{ZF}_{\text{fin}}$  is an  $\omega$ -model. (Received August 05, 2008)