Let $PEP$ be the class of proper essential $P$-spaces, i.e. spaces with exactly one non-$P$-point, and let $PEP_\delta$ be the class of $PEP$-spaces whose non-$P$-point is a $G_\delta$. The $l$-groups $C(X)$ with $X \in PEP$ are often non-projectable and in [1] it is shown that many of those with $X \in PEP_\delta$ have decidable theories. We discuss analogous results for $C(X)$ with $X \in PEP - PEP_\delta$.