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A *quasiconformal group* is a discrete group of quasiconformal automorphisms of the unit disk  $\Delta$  whose maximal dilations are uniformly bounded. A quasisymmetric automorphism of the unit circle  $\partial\Delta$  is the boundary extension of a quasiconformal automorphism of  $\Delta$ . A *quasisymmetric group* is a discrete group of quasisymmetric automorphisms of  $\partial\Delta$  whose quasisymmetric constants are uniformly bounded. Markovic has proved that every quasisymmetric group is conjugate to a Fuchsian group by a quasisymmetric homeomorphism  $\partial\Delta \rightarrow \partial\Delta$ , or equivalently, every quasisymmetric group is the boundary extension of a quasiconformal group.

An *asymptotically conformal group* is a quasiconformal group whose elements are asymptotically conformal automorphisms of  $\Delta$ . A symmetric automorphism of  $\partial\Delta$  is the boundary extension of an asymptotically conformal automorphism of  $\Delta$ . A *symmetric group* is a quasisymmetric group whose elements are symmetric automorphisms of  $\partial\Delta$ . In this talk, we consider a problem whether a symmetric group is conjugate to a Fuchsian group by a symmetric homeomorphism  $\partial\Delta \rightarrow \partial\Delta$  or not. (Received August 19, 2008)