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It is well known that the squares of elements in a group do not form a subgroup and that the alternating group on four letters is minimal with this property. For given n , what is the group of minimal order such that the n -th powers of elements do not form a subgroup? For odd n , it can be shown that the dihedral group of order $2p$ is minimal with this property, where p is the smallest prime dividing n .

If n is even, the situation is more complex. The order of the group of minimal order with this property depends on the odd prime factors of n and the exact 2-power dividing n . With initial guidance from GAP, we determine the groups of minimal order such that the n -th powers do not form a subgroup in case $n = 2k, 4k$, and $8k$, where k is odd. (Received July 28, 2008)