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Scott M Bailey*, University of Rochester, Department of Mathematics, R.C. Box 270138,
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The root invariant of Mahowald associates to every element α in the stable homotopy groups of spheres, another element $R(\alpha)$. Since the construction introduces indeterminacy, the root invariant is a coset in general. Ravenel and Mahowald conjectured that the root invariant of a v_n -periodic element is v_{n+1} -periodic. Furthermore, they continued to exhibit a relationship between elements that were themselves root invariants with their behavior in the EHP spectral sequence. In particular, $R(-)$ seems to provide an interesting connection between the unstable world and chromatic view of the stable world. Although neither a proof, nor a precise statement, of this phenomena exists there are computations establishing its plausibility. For example, the construction of the root invariant is closely related to that of the Tate spectrum, tE , of a spectrum E . Numerous authors have given examples of v_n -periodic cohomology theories (*bo*, $BP\langle 2 \rangle$, Johnson-Wilson theories $E(n)$, etc.) which become v_n -torsion under the Tate spectrum construction. In this talk, I will define the Tate spectrum functor, and discuss a similar splitting of $t(tm f)$ at the prime 2. (Received August 11, 2008)