

1044-05-147

**Linyuan Lu** and **Yi Zhao\*** (yzhao6@gsu.edu), Dept of Math & Stat, P.O. Box 4110, Atlanta, GA 30302. *On the upper bound for the Turán density of  $K_{r+1}^r$ .*

We first prove an exact result for hypergraphs: given  $r \geq 3$ , let  $p$  be the smallest prime factor of  $r - 1$ . Let  $G = (V, E)$  be an  $r$ -uniform hypergraph on  $n$  vertices such that every  $r + 1$  vertices contain 0 or  $r$  edges. If  $n > (p - 1)r$ , then either  $E = \emptyset$  or  $E = \{S \subset V : |S| = r, S \ni x\}$  for some  $x \in V$ . We then use it to show that the Turán density

$$\pi(K_{r+1}^r) \leq 1 - \frac{1}{r} - \frac{1}{2r^{2p-3}}$$

for all even  $r \geq 4$ , improving a well-known upper bound  $1 - \frac{1}{r}$  of de Caen and Sidorenko. (Received August 29, 2008)