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Michael Ferrara, Colton Magnant and Jeffrey Powell* (JSPOWEL1@samford.edu), Dept. of Mathematics & Computer Science, 800 Lakeshore Drive, Birmingham, AL 35229. *Minimum Degree Conditions for Subdivision Extensions and Pan- H -linked Graphs.*

For a multigraph H , an H -subdivision is any graph obtained by replacing the edges of H with paths of arbitrary length. Many well-known minimum degree results in graph theory give the minimum degree needed to either increase the order of an embedded subdivision by one vertex (e.g. panconnected, pancyclic) or to find a spanning H -subdivision (e.g. Dirac's Theorem where H is a loop). For the spanning subdivision case, a recent result by Gould and Whalen states that if $\delta(G) \geq \frac{n+m-k+n_1(H)+2n_0(H)}{2}$, then there exists a spanning subdivision of H in G . Their result has Dirac's Theorem as a corollary.

In this talk, we focus on increasing the order of subdivisions by one vertex. In particular, we present a result that shows that for most graphs H , the exact same minimum degree condition above implies that any H -subdivision on a particular ground set of vertices can be extended to an H -subdivision on the same ground set containing one more vertex. This result is in the spirit of Bondy's result that Dirac's condition ($\delta(G) \geq \frac{n}{2}$) also implies that G is either pancyclic or a complete bipartite graph. The concept of a pan- H -linked graph, which is a generalization of pancyclic and panconnected graphs, is introduced as well. (Received September 02, 2008)