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Alexandru Gabriel Atim* (atimg@gwm.sc.edu), USC Lancaster, P O Box 889, Lancaster, SC 29721, and **Robert R Kallman**. *The Polish Group Topology on the Unitary Group is Unique.*

Let \mathcal{H} be an infinite dimensional separable Hilbert space, $\mathcal{U}(\mathcal{H})$ the unitary group acting on \mathcal{H} , G a complete separable metric topological group and $\phi : G \rightarrow \mathcal{U}(\mathcal{H})$ an algebraic isomorphism. Then ϕ is a topological isomorphism. The theorem is false for $\mathcal{U}(\mathcal{H})$ if \mathcal{H} is finite dimensional. If \mathcal{H} is a real infinite dimensional separable Hilbert space, the theorem is true for the orthogonal group $\mathcal{O}(\mathcal{H})$. Similar theorems hold for the associated projective groups. (Received September 02, 2008)