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**Georg Hetzer\*** ([hetzege@auburn.edu](mailto:hetzege@auburn.edu)), Department of Mathematics and Statistics, 304 Parker Hall, Auburn University, AL. *Positive Solutions for a Class of Set-Valued Functional Evolution Equations*. Preliminary report.

Let  $X$  be a reflexive ordered Banach space with uniform convex dual,  $M$  be a complete metric space, and  $C(M) \hookrightarrow X$  (compactly). The existence of positive global bounded solutions will be discussed for the initial value problem

$$\begin{cases} \dot{u} + Au \in F(t, u_t, V(u|_{[0,\infty)})) & t > 0, \\ u(s) = u_0(s) \geq 0 & -T \leq s \leq 0, \end{cases}$$

where  $A : \mathfrak{D}(A) \subset C(M) \rightarrow X$  is  $m$ -accretive,  $-A$  generates a compact semigroup in  $X$ , and the resolvent of  $A$  maps the positive cone of  $X$  into itself.  $F : \mathbb{R}_+ \times C([-T, 0], C(M, \mathbb{R}_+)) \times Z^+ \rightarrow 2^X \setminus \{\emptyset\}$  is, loosely stated, an upper semi-continuous set-valued map, which is “positive” near  $u = 0$  and is “negative” near  $u = \infty$ .  $Z$  denotes a Banach space with positive cone  $Z^+$  which is densely embedded in  $C(M, \mathbb{R}_+^m)$  ( $m \in \mathbb{N}$ ), and  $V : C_b([0, \infty), C(M, \mathbb{R}_+)) \rightarrow C_b([0, \infty), Z^+)$  is in particular continuous and has the Volterra property. (Received August 25, 2008)