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Wladyslaw Kulpa and **Andrzej Szymanski*** (andrzej.szymanski@sru.edu), Department of Mathematics, Slippery Rock University, Slippery Rock, PA 16057. *On L^* -spaces.*

An L^* -operator on a topological space X is a function $\Lambda : [X]^{<\omega} - \{\emptyset\} \rightarrow 2^X$ satisfying the following condition:

(*) If $A \in [X]^{<\omega} - \{\emptyset\}$ and $\{U_x : x \in A\}$ is an open cover of X , then there exists $\emptyset \neq B \subseteq A$ such that $\Lambda(B) \cap \bigcap \{U_x : x \in B\} \neq \emptyset$.

The family $\mathbf{Con}(\Lambda) = \{Y \subseteq X : \Lambda(B) \subseteq Y \text{ for each } B \in [Y]^{<\omega} - \{\emptyset\}\}$ is a convexity structure on X . It constitutes a proper generalization of well exploited L -structures defined by Ben-El-Mechaiekh, Chebbi, and Florenzano in 1998. We show that if X is a connected LOTS, then $\Lambda(A) = [\min A; \max A]$ defines an L^* -operator on X and that the convexity structure $\mathbf{Con}(\Lambda)$ cannot be an L -structure in case X is a connected Souslin line. We prove fixed point and equilibrium theorems for spaces that admit continuous L^* -operators. (Received August 26, 2008)