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Robert W. Heath* (rwheath@pitt.edu), 1223 Whisper Ridge Rd., Auburn, AL 36830, and
Thomas J. Poerio. *Topological Algebraic Structure on \mathbb{R} with The Density Topology.* Preliminary report.

The density of a subset E of \mathbb{R} at a point x is defined to be the limit, as h goes to 0, of $\frac{m_1(E \cap (x-h, x+h))}{2h}$. In the density topology a set is open if the density of the set is 1 at each of its points. Tall [Pacific Journal, 1976] showed that a subset of \mathbb{R} is connected in the density topology iff it is connected in the open interval topology. We use Hugo Steinhaus's theorem (Fundamenta, 1920) to show that neither $\{\mathbb{R}, +\}$ nor $\{\mathbb{R}^+, x\}$ can be a cancellative topological semigroup in the density topology. Further we show that there can be no cancellative topological semigroup on \mathbb{R} with the density topology. (Received August 29, 2008)