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**Zbigniew Piotrowski\*** (zpiotr@math.ysu.edu), Youngstown State University, Department of Mathematics, One University Plaza, Youngstown, OH 44555, and **Eric J. Wingler**. *An Extension of the Closed Graph Theorem for Separately Continuous Functions*. Preliminary report.

In 1991 we have showed [Real Analysis Exchange] the following Theorem: Let  $X$  and  $Y$  be topological spaces with  $Y$  being locally connected and  $Z$  locally compact. Then any closed graph function  $f : X \times Y \rightarrow Z$  having continuous  $y$ -sections and connected  $x$ -sections, is continuous. Hence, as an immediate consequence we have that if  $X$  is locally connected,  $Y$  is locally compact and  $f : X \rightarrow Y$  is a connected mapping with closed graph, then  $f$  is continuous. (apply the theorem to the function  $f^* : 0 \times X \rightarrow Y$ , defined by  $f^*(0,x) = f(x)$ ). In 2005, M.R.Wojcik and M.S.Wojcik [Real Analysis Exchange 30] generalized the above result keeping the same assumptions on the considered spaces and  $x$ -sections, but relaxing the condition on  $y$ -sections to "at least one section is continuous". Knowing that connected and closed graph functions  $f : \mathbb{R} \rightarrow \mathbb{R}$  are continuous, they asked whether this result is also true for real-valued functions defined on the plane. Jiri Jelinek [Acta Univ.Carolin.Math.Phys.44(2003)] answered this question, in the negative, by constructing a clever, yet elementary example of a discontinuous connected closed graph real-valued function from the plane. We will generalize our Theorem by relaxing the closed graph condition to closed fibres (= preimages of points are closed) (Received August 30, 2008)