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David Lutzer* (lutzer@math.wm.edu), Mathematics Department, College of William and Mary, Williamsburg, VA 23187-8795. *Completeness, domain representability, and measurements.*

I will report on recent work that Harold Bennett and I did on representability and on measurement problems in domains and Scott domains. A preprint is available on my webpage at <http://www.math.wm.edu>.

We show that if a space X is representable as $X = \max(D)$ where $\max(D)$ is a G_δ -subset of a domain D , then X is first-countable and is the union of a family of dense completely metrizable subspaces, and we show that $[0, \omega_1)$ is representable in this way. We show that if $Y = \max(S)$ is a G_δ in a Scott domain S , then Y is weakly developable (in the sense of Alleche, Arhangel'skii, and Calbrix) and has a G_δ diagonal. Consequently it is not possible that $[0, \omega_1) = \max(S)$ is a G_δ in a Scott domain S , and this corrects a mistake in the literature.

We show that Burke's non-developable, locally compact Hausdorff space with a G_δ -diagonal is homeomorphic to $\max(S)$ where S is a Scott domain in which $\max(S)$ is a G_δ -subset of S , and yet no measurement μ on S has $\ker(\mu) = \max(S)$. Finally we show that the kernel of a measurement on a Scott domain can consistently be a normal, separable, non-metrizable Moore space. (Received August 22, 2008)