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**Scott M Bailey\*** ([bailey@math.rochester.edu](mailto:bailey@math.rochester.edu)), University of Rochester, Department of Mathematics, R.C. Box 270138, Rochester, NY 14626. *On the Tate spectrum of  $tmf$  at the prime 2*. Preliminary report.

The root invariant of Mahowald associates to every element  $\alpha$  in the stable homotopy groups of spheres, another element  $R(\alpha)$ . Since its construction introduces indeterminacy, the root invariant is a coset in general. Ravenel and Mahowald conjectured that the root invariant of a  $v_n$ -periodic element is  $v_{n+1}$ -periodic. Furthermore, they continued to exhibit a relationship between elements that were themselves root invariants with their behavior in the EHP spectral sequence. In particular,  $R(-)$  seems to provide an interesting connection between the unstable world and the chromatic view of the stable world. Although neither a proof, nor a precise statement, of this phenomena exists there are computations establishing its plausibility. For example, the root invariant is closely related to that of the Tate spectrum,  $tE$ , of a spectrum  $E$ . Numerous authors have given examples of  $v_n$ -periodic cohomology theories ( $bo$ ,  $BP\langle 2 \rangle$ , Johnson-Wilson theories  $E(n)$ , etc.) which split into  $v_n$ -torsion after the Tate spectrum functor is applied. In this talk, I will define the Tate spectrum functor, and discuss a similar phenomena of  $t(tm f)$  at the prime 2. (Received August 26, 2008)