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**George W Patrick\*** ([patrick@math.usask.ca](mailto:patrick@math.usask.ca)), Department of Mathematics and Statistics,  
University of Saskatchewan, Saskatoon, SK S7N 5E6, Canada. *Local error analysis of variational  
integrators.*

Discretizations of variational principles of physical systems are towards discrete models that have a status equivalent to the continuous models. For Hamilton's principle of mechanics, such discretizations lead to a class of numerical methods called variational integrators. Existence and uniqueness, and accuracy, of variational integrators, cannot be correctly established without due consideration of their singularities at zero time-step. We show existence and uniqueness for variational integrators by blowing up the variational principle at zero time-step. This gives an accuracy one less than is observed in simulations, a deficit that is recovered by a past–future symmetry of the blown-up principle. (Received August 31, 2008)