

1047-05-339

Jozsef Balogh and **Wojciech Samotij*** (samotij2@illinois.edu). *Counting graphs without a fixed subgraph.*

A graph is called H -free if it contains no copy of H . Denote by $f_n(H)$ the number of (labeled) H -free graphs on n vertices. Since every subgraph of an H -free graph is also H -free, it immediately follows that $f_n(H) \geq 2^{ex(n,H)}$. Erdős conjectured that, provided H contains a cycle, this trivial lower bound is in fact tight, i.e.

$$f_n(H) = 2^{(1+o(1))ex(n,H)}.$$

The conjecture was resolved in the affirmative for graphs with chromatic number at least 3 by Erdős, Frankl and Rödl (1986), but the case when H is bipartite remains wide open. We will give an overview of the results in case $\chi(H) = 2$, and talk about a few related problems and recent progress in the area. (Received February 02, 2009)