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**Dimitris Koukoulopoulos\*** (dkoukou2@illinois.edu), Department of Mathematics, University of Illinois at Urbana-Champaign, Urbana, IL 61801. *Generalized multiplication tables.*

Fix  $k \geq 2$ . For  $N_1, \dots, N_k$  integers consider the  $k$ -dimensional multiplication table formed by taking all products  $n_1 \cdots n_k$  with  $n_i \leq N_i$ ,  $1 \leq i \leq k$ . Let  $A_k(N_1, \dots, N_k)$  be the number of distinct integers that appear in this table. We seek bounds on  $A_k(N_1, \dots, N_k)$ . In 2004 Ford established the order of magnitude of  $A_2(N, N)$ . We generalize Ford's result by determining the order of magnitude of  $A_k(N, \dots, N)$  when  $k > 2$ . Finally, we investigate how  $A_3(N_1, N_2, N_3)$  behaves when the sizes of  $N_1, N_2, N_3$  start varying. (Received February 03, 2009)