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Let  $\mathbb{R}[X] = \mathbb{R}[X_1, \dots, X_n]$  and let  $\Delta_n$  denote the standard  $n$ -simplex  $\{(x_1, \dots, x_n) \in \mathbb{R}^n \mid x_i \geq 0, \sum_i x_i = 1\}$ . Pólya's Theorem says that if a form (homogeneous polynomial)  $p \in \mathbb{R}[X]$  is positive on  $\Delta_n$ , then for sufficiently large  $N \in \mathbb{N}$ , the coefficients of  $(X_1 + \dots + X_n)^N p$  are positive. In this talk, we discuss a generalization of Pólya's Theorem to forms which are allowed to have zeros in the simplex. We give a characterization of forms which satisfy the conclusion of Pólya's Theorem (with "positive coefficients" replaced by "nonnegative coefficients") and give a bound for the  $N$  needed. (Received February 02, 2009)