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**Lev Glebsky\*** (glebsky@cactus.iico.uaslp.mx), Department of Math., University of Illinois at Urbana-Champaign, 1409 West Green Street, Urbana, IL 61801, and **L.M. Rivera**. *Sofic groups and profinite topology on free groups*.

The notion of sofic groups was introduced by M. Gromov in relation with the "surjunctivity" problem of cellular automata due to Gottschalk. It is an open question if there is a non-sofic group. We show the relation of sofic groups with the profinite topology on a free group.

We give a definition of weakly sofic groups (w-sofic groups). Our definition is a rather natural extension of the definition of sofic groups where instead of the Hamming metric on symmetric groups we use general bi-invariant metrics on finite groups. Let  $F$  be a finitely generated free group and  $N \triangleleft F$ . Then  $F/N$  is w-sofic if and only if for any finite sequence  $g_1, g_2, \dots, g_k \in N$  one has  $\overline{[g_1]^F [g_2]^F \dots [g_k]^F} \subseteq N$ . Where  $\overline{X}$  denotes the closure of  $X$  in the profinite topology on  $F$ . (Received February 02, 2009)