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**Albert Baernstein II\*** (al@math.wustl.edu), Math, Washington University, St.Louis, MO 63130, and **A. Yu Solynin**. *Monotonicity and comparison results for conformal invariants*. Preliminary report.

Suppose that  $\Omega$  is an  $n$ -fold symmetric domain in the plane and that  $u$  is a function in the plane which satisfies a differential inequality  $\Delta u \geq \gamma(u) + f$  in  $\Omega$ . Assume also that  $u$  is constant outside  $\Omega$ . We prove that if  $\gamma$  and  $f$  satisfy certain conditions, among them that  $f$  be  $n$ -fold symmetric, then  $u$  is  $n$ -fold symmetric. We prove also that if  $u$  is desymmetrized in a certain way, then the function thus obtained is majorized by a function  $v$  which satisfies  $\Delta v \leq \gamma(v) + f_1$ , where  $f_1$  is a corresponding desymmetrization of  $f$ . These results permit us to solve some extremal problems involving Poincaré metrics, harmonic measure and capacities. (Received January 27, 2009)