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Quanhua Xu* (qxu@univ-fcomte.fr), Laboratoire de Mathematiques, Universite de Franche-Comte, 25030 Besancon, France. *Structures of certain homogeneous Hilbertian operator spaces and applications.*

Let $QS(C \oplus R)$ denote the class of quotients of subspaces of $C \oplus R$. We show that the operator space structure of each homogeneous $F \in QS(C \oplus R)$ is completely determined, under a mild regularity assumption, by its fundamental sequences

$$\Phi_c(n) = \left\| \sum_{k=1}^n e_{k1} \otimes e_k \right\|_{C \otimes_{\min} F}^2, \quad \Phi_r(n) = \left\| \sum_{k=1}^n e_{1k} \otimes e_k \right\|_{R \otimes_{\min} F}^2,$$

where (e_k) is an orthonormal basis of F . The underlying result is a canonical representation of F in terms of weighted column and row spaces with weights given by Φ_c and Φ_r . This canonical representation yields an explicit formula for the exactness constant of an n -dimensional subspace F_n of F :

$$ex(F_n) \sim \left[\frac{n}{\Phi_c(n)} \Phi_r\left(\frac{\Phi_c(n)}{\Phi_r(n)}\right) + \frac{n}{\Phi_r(n)} \Phi_c\left(\frac{\Phi_r(n)}{\Phi_c(n)}\right) \right]^{1/2}.$$

The projection constant of F_n is explicitly expressed in terms of Φ_c and Φ_r too. Orlicz space techniques play a crucial role in our arguments. They also permit to determine the completely 1-summing maps between two homogeneous spaces E and F in $QS(C \oplus R)$. This is a joint work with Marius Junge. (Received February 02, 2009)