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**Christian Le Merdy\*** ([clemerdy@univ-fcomte.fr](mailto:clemerdy@univ-fcomte.fr)), Laboratoire de Mathematiques, Universite de Franche-Comte, Besancon Cedex, 25030. *Group representations and  $R$ -boundedness.*

Let  $G$  be an amenable group and let  $C^*(G)$  be its associated group  $C^*$ -algebra. Let  $X$  be a Banach space and let  $\pi: G \rightarrow B(X)$  be a bounded continuous representation. A well-known theorem (Nagy, Dixmier) asserts that if  $X = H$  is a Hilbert space, then  $\pi$  is similar to a unitary representation. Equivalently,  $\pi$  naturally extends to a bounded unital homomorphism  $C^*(G) \rightarrow B(H)$ . Our main result is an extension of this result to the Banach space setting. Under some mild conditions on  $X$ , it says that if  $\pi$  is  $R$ -bounded, then it extends to a bounded unital homomorphism  $\widehat{\pi}: C^*(G) \rightarrow B(X)$ . The notion of  $R$ -boundedness relies on Rademacher averages in Banach spaces and will be defined during the talk. If time permits, we will explore more relationships between operator algebras, Banach space homomorphisms and  $R$ -boundedness. (Received January 30, 2009)