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Iowa City, IA 52242. *Cubic Column Relations in Truncated Moment Problems*. Preliminary report.

For a degree  $2n$  real  $d$ -dimensional multisequence  $\beta \equiv \beta^{(2n)} = \{\beta_i\}_{i \in \mathbb{Z}_+^d, |i| \leq 2n}$  to have a representing measure  $\mu$ , it is necessary for the associated moment matrix  $M(n)$  to be positive semidefinite, and for the algebraic variety associated to  $\beta$ ,  $V_\beta$ , to satisfy  $\text{rank } M(n) \leq \text{card } V_\beta$  as well as the following consistency condition: if a polynomial  $p(x) \equiv \sum_{|i| \leq 2n} a_i x^i$  vanishes on  $V_\beta$ , then  $p(\beta) := \sum_{|i| \leq 2n} a_i \beta_i = 0$ . In previous joint work with L. Fialkow and M. Möller, we proved that for the extremal case ( $\text{rank } M(n) = \text{card } V_\beta$ ), positivity and consistency are sufficient for the existence of a (unique, rank  $M(n)$ -atomic) representing measure.

In recent joint work with Seonguk Yoo we consider cubic column relations in  $M(3)$  of the form (in complex notation)  $Z^3 = itZ + u\bar{Z}$ , where  $u$  and  $t$  are real numbers. For  $(u, t)$  in the interior of a real cone, we prove that the algebraic variety consists of exactly 7 points, and we then apply the above mentioned solution of the extremal moment problem to obtain a necessary and sufficient condition for the existence of a representing measure. (Received February 03, 2009)