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Robert Lee Wilson* (rwilson@math.rutgers.edu), Rutgers University, Department of Mathematics, Piscataway, NJ 08854-8019. *Multisum identities related to $A_1^{(1)}$* . Preliminary report.

Let $k, k_0, k_1 \geq 0$ be integers with $k_0 \leq k - 1$ and $k_0 + k_1 = 2k - 1$. Then the principally specialized character of the vacuum space for the standard $A_1^{(1)}$ -module with highest weight $\Lambda = k_0\Lambda_0 + k_1\Lambda_1$ may be expressed (by a result of Gordon) as an infinite sum $\sum_{m \geq 0} |A(k, k_0, m)|q^m$ where $A(k, k_0, m)$ is the set of partitions (a_1, \dots, a_s) of m satisfying $a_1 \geq a_2 \geq \dots \geq a_s, a_i - a_{i+k-1} \geq 2 \ \forall i, 1 \leq i \leq s - k + 1$, and $a_{s-k_0} > 1$. It may also be expressed (by a result of Andrews) as a multisum. We relate these two expressions using the operators $X^{(i)}$ introduced by Meurman and Primc on the standard $A_1^{(1)}$ -module V_Λ . (Received February 10, 2009)